

Case Studies in the Assessment of Rock Mass Criteria

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Summary Various rock mass failure criteria are being validated against field performance as part of a large research program into the geotechnical risk of concrete gravity dams. The project has sought rock structures which may contribute to providing either upper or lower bounds to various failure criteria. The emphasis therefore has been on finding sites with high quality field and laboratory data. This paper summarises the analysis and results of a large pit slope at Kidston Gold Mine, together with a summary of other previously reported cases. The results from the studies allow the field stresses and strengths to be compared with the commonly used Hoek-Brown empirical rock mass failure criterion. As expected, the bounds on the various failure criteria are very broad and care must be taken when placing any reliance on any particular criterion.

1 INTRODUCTION

The author is currently involved with a research project into the risk assessment of concrete dams. A major component of this project is to attempt to validate various rock mass failure criteria against field performance. An extensive literature review has shown that almost all the data supporting the published criteria are laboratory test results from intact specimens, with, in general, very little and often no field validation. Rock mass strength is clearly scale dependent and thus laboratory testing alone cannot be expected to have captured important field characteristics.

The most commonly used strength criterion is the Hoek-Brown empirical rock mass failure criterion. The most general form of which is given in Equation (1). This criterion was developed by Hoek and Brown (1) due to the lack of any available empirical strength criterion. The equation which has subsequently been updated by Hoek and Brown (2) and Hoek et. al. (3) was based on correlations between brittle fracture of intact rock cores and the original Griffith theory (4). The only 'rock mass' tested and used in the development of the Hoek-Brown criterion was 152mm core samples of Panguna Andesite from Bougainville in Papua New Guinea (1). Brown and Hoek (5) later noted that it was likely this material was in fact 'disturbed'. The validation of the updates of the Hoek-Brown criterion have been based on experience gained whilst using this criterion. It is unfortunate however, that to the authors knowledge the data supporting this experience has not been published.

$$\sigma_1' = \sigma_3' + \sigma_c \left(m_b \frac{\sigma_3'}{\sigma_c} + s \right)^a \quad (1)$$

Due to the difficulty with assessing the parameters in the Hoek-Brown criterion correlations with rock mass rating parameters were developed. The most current of these is the Geological Strength Index (GSI) (6) which is a variation on the rock mass rating (RMR) of Bieniawski (7 and 8) and the tunneling quality index (Q) of Barton et al. (9). These are shown in Table 1. The parameters m_i and m_b are intact and mass material constants; a and s are constants that depend on the rock mass characteristics; σ_c is the uniaxial compressive strength of the intact rock; and σ_1' and σ_3' are the major and minor principal stresses respectively.

	GSI<25	GSI>25
$\frac{m_b}{m_i}$	$\exp\left(\frac{GSI-100}{28}\right)$	$\exp\left(\frac{GSI-100}{28}\right)$
s	0	$\exp\left(\frac{GSI-100}{9}\right)$
a	$a = 0.65 - \frac{GSI}{200}$	0.5

Table 1: Hoek-Brown GSI Strength Parameters

This paper describes some of the authors work in attempting to correlate field data to the Hoek-Brown criterion. Results from several case studies are shown.

2 KIDSTON GOLD MINE

The footwall of the Wises Hill pit, located at Kidston Gold Mine, Queensland, is approximately 240m high. The average slope angle is approximately 48° with a maximum bench height and slope of approximately 36m and 73° respectively. The pit has been successfully mined with no overall stability problems. The pit was chosen for analysis due to its highly

stressed nature. An analysis using the stability program *Slope/W* has been performed and the stresses obtained compared with those output from the Hoek-Brown criterion.

2.1 Rock Parameters

The major rock type in the slope is a very high strength granodiorite breccia. Rock mass parameters were obtained from Coffey Partners International Pty Ltd (10) and line mapping histograms created by Pells Sullivan Meynink Pty Ltd (PSM). Estimates of GSI were derived using RMR₇₆, Q, Table 8.4 in Hoek et. al. (11) and Figure 1 in Hoek (12). The value of m_i for granodiorite was taken from Hoek et. al. (11). The Hoek-Brown parameters are shown in Table 2. Three estimates were made: LB being the lower bound; BE being the best estimate; and UB being the upper bound.

Parameter	LB	BE	UB
GSI (RMR ₇₆)	77	82	92
GSI (Q)	72	72	73
GSI (Table 8.4)	70	70	85
GSI (Figure 1)	60	65	75
UCS	100	100	120
m_i	30	30	30
a	0.5	0.5	0.5

Table 2: Hoek Parameters for Kidston

As can be seen in Table 2 the value of GSI varies considerably depending on the method used to derive it. The latest approach by Hoek (12) gives the lowest estimate. Indeed, an inspection of this method shows that the highest possible GSI is 80 for a 'blocky structure' with 'very good surface conditions'. Due to this variation it is suggested that those using the criterion make sure they are using the latest update for the estimation of GSI and the Hoek-Brown criterion.

2.3 Slope Stability Analysis

The stability program *Slope/W* was used for the analysis with both Bishop and Morgenstern & Price analyses. The parameters used are shown in Table 3. They were obtained using the Hoek-Brown strength criterion and the solutions derived by Balmer (13) with a linear interpolation of the points in the stress region of interest.

Parameter	GSI=60	GSI=70	GSI=92
m_b	7.2	10.3	22.5
ϕ (°)	67	68	68
c (MPa)	1.2	1.9	6.7

Table 3: Results of Hoek-Brown Analysis ($\sigma_n = 0.8\text{MPa}$)

It should be noted that the suggested values of minimum principle stress, σ_3 , given by Hoek et. al. (11) for use in their spreadsheet are applicable more to highly stressed underground workings than slopes. The high cohesions of rock masses result in negative σ_3 being required to obtain

low σ_n on potential failure planes. Users should use stress, which yield normal stresses, σ_n , applicable to their problem. The values for the cohesion, c , and angle of friction, ϕ , in Table 3 assume a normal stress of 0.8MPa. This normal stress was determined iteratively using the slice base normal forces output from *Slope/W* and adjusting the parameters accordingly.

Both a deep failure surface and a shallower failure surface incorporating only the steeper section of the pit were analysed. For the deep failure surface the slope was modelled as three material types with the least stressed upper and lower materials given a slightly lower strength ($\sigma_n = 0.8\text{MPa}$ used) compared to that of the middle layer ($\sigma_n = 1.2\text{MPa}$).

A further analysis was carried out to assess the effect a joint would have if it occurred at the toe of the slope. This was justified from the line mapping results by PSM which showed the presence of long joints (5-10% greater than 50m) in the region of the toe. To carry out the analysis a zone of material with joint strength properties was added in the location of the toe of the shallow failure slip surface. The joint strength properties, of zero cohesion and an angle of friction, ϕ , of 40°, were taken from Coffey Partners International (10). The weak 'joint' material was stopped short of the face due to the presence of rock bolting in the face at Kidston.

Tension cracks were added for all analyses at the top of the failure surfaces to limit tension.

2.4 Results

Figures 1, 2 and 3 show the failure surfaces for the deep, shallow and joint material analyses respectively. The analyses through the rock masses gave a FOS of approximately 6.5. The analysis where the joint region was included yielded a FOS of 4.9. Lower factors of safety were obtained for other surfaces but were rejected due to the shallow nature or excessive tensile stresses between slices.

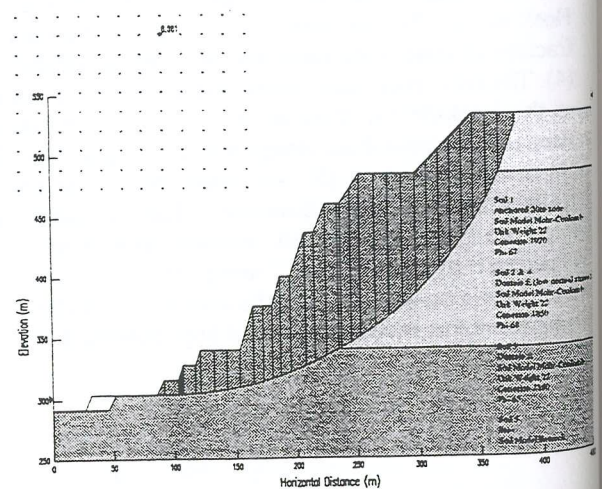


Figure 1: Deep Seated Failure - Kidston Mine

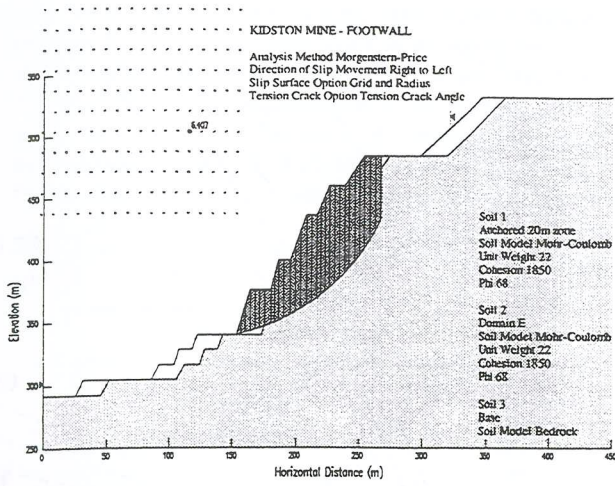


Figure 2: Shallow Failure Surface - Kidston Mine

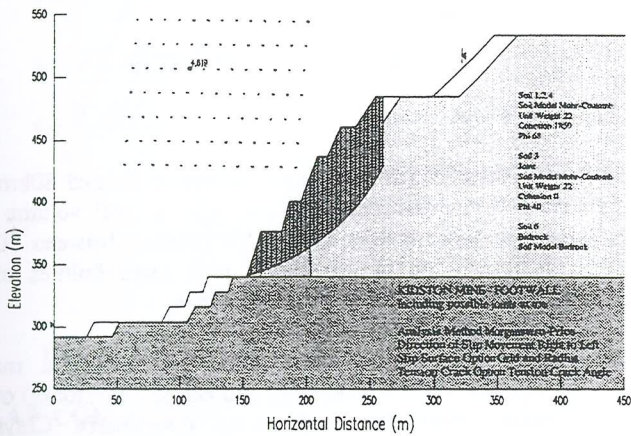


Figure 3: Failure Through Joint Region - Kidston Mine

The slice base normal and shear stresses are plotted on Figure 4 together with the Hoek-Brown criterion curves for the lower bound, best estimate and upper bound GSI values (60, 70 and 92 respectively). Figure 4 shows that although the slope appears highly stressed it does not appear to be a very good bound for rock mass strength.

It is difficult to imagine rock mass behaviour leading to failure for slopes with a high GSI rock mass. Using the best estimate rock mass strengths output by the Hoek-Brown criterion for Kidston a quick analysis with *Slope/W* showed a 70° slope could be over 5000m high without inducing failure.

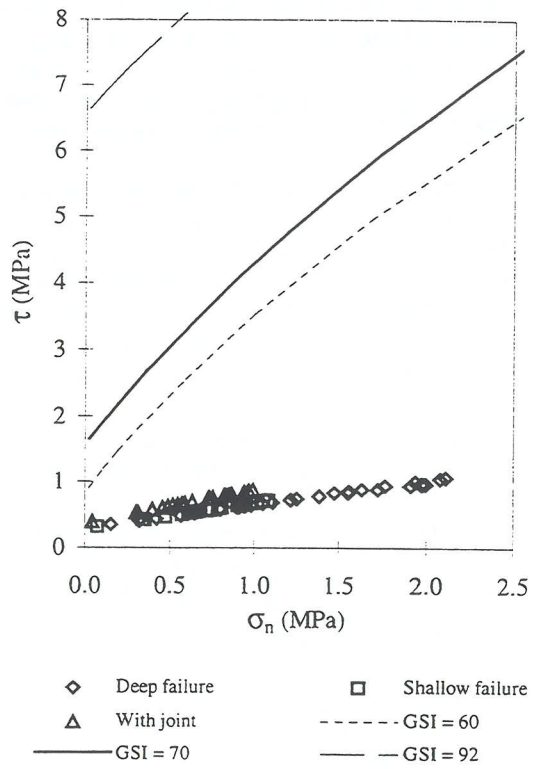


Figure 4: Hoek-Brown vs Stresses for Kidston

3.0 OTHER CASE STUDIES

3.1 Aviemore Dam

Aviemore Dam, a 57m high concrete dam constructed between 1963 and 1968, is located on the Waitaki River, 185km south west of Christchurch, New Zealand. During construction eight large scale in-situ shear tests were carried out on the foundation in order to determine the strength of the concrete/rock interface for stresses relevant to those induced by the proposed dam.

The in-situ tests were carried out on a greywacke rock mass which was closely jointed, veined, and often crushed and sheared. All tests failed through the rock mass, approximately 50-100mm below the rock-concrete contact, involving failure of several defects.

During the tests both the test and reaction blocks failed. Foster and Fairless (14) re-analysed the test results and adjusted the vertical stresses on the test and reaction blocks assuming that vertical forces were transferred from the reaction block to the test block due to differential displacement. The values were adjusted to yield similar τ/σ_n ratios for the reaction and the test blocks. Their results have been adopted as a best estimate of the true failure stresses. By using *UDEC* Helgstedt et. al. (15) found it was possible to validate the assumptions made by Foster and Fairless (14) and thus provide a greater confidence in their results.

The test results are presented in Figure 5 together with the estimated Hoek-Brown envelopes. As can be seen the best estimate Hoek-Brown criterion gave a higher estimate of the rock mass strength compared with the adjusted test values. The failure stresses appear to correspond reasonably to the lower bound estimated Hoek-Brown envelope.

The Hoek-Brown curves derived using the chart in Hoek (6) give a lower estimate of the rock mass strength. The Hoek-Brown curves derived using Barton's Q system give higher estimates than those from Bieniawski's RMR₈₉ and the Hoek-Brown chart in Hoek et. al. (11). It appears from the results that the curves derived from the Hoek-Brown chart give the best estimate of the rock mass strength.

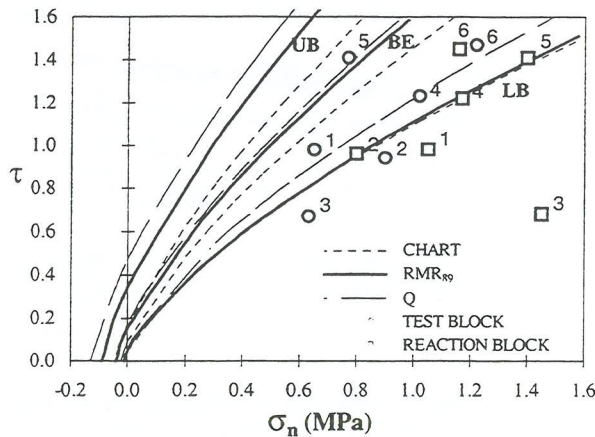


Figure 5: Aviemore In-Situ Shear Test Results

3.2 Chichester Dam

Chichester Dam is a 41m high concrete gravity dam located on the Chichester River, 80km north of Newcastle, NSW. The dam has been heavily investigated with approximately 150 boreholes drilled between 1950 and 1980. As a result of these investigations, the dam was post tensioned to provide additional security against extreme hydrological events.

The parameters used in the analysis are described in detail in Mostyn et. al. (16). The dam foundation was modelled using UDEC. The results from the analysis are shown in Figure 6.

The results from the analysis indicated that a planar wedge failure was the likely failure mode and hence the Hoek-Brown criterion was not applicable. The analysis also showed that the low stresses beneath a dam of this size are not conducive to placing tight bounds on rock mass strength criteria.

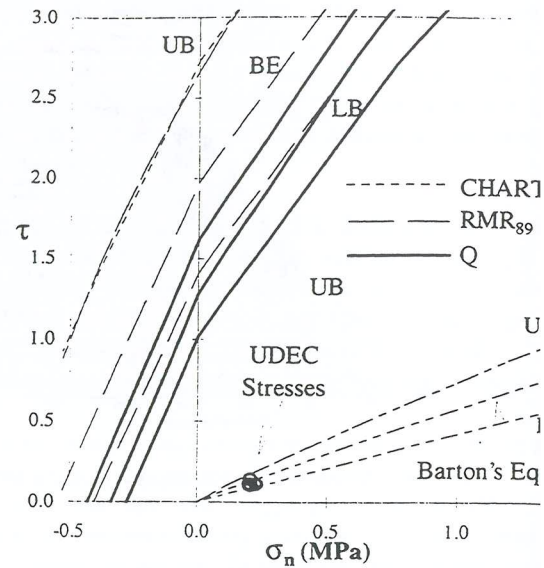


Figure 6: Chichester Dam Results

3.3 Nattai North

The Nattai North escarpment failure is located 80km west of Sydney. The failure, with a total volume million cubic meters and height ranging between 200 and 300m, is one of the largest rock mass failures occurred in Australia in modern times.

The conditions at Nattai North are such that competent rock (Scarborough and Bulgo Sandstones) weaker, more fractured strata (Wombarra Claystone). Together with this, the bedding planes tend to dip steeply, resulting in large pillars that are prevented from sliding or toppling. These pillars are then supported by highly stressed weaker Wombarra Claystone. The conditions are believed to be sufficient to cause failure through the claystone and failure of the escarpment. It is believed that the failure was induced by mining of coal beneath the escarpment.

The modelling of the failure was performed using UDEC. Two series of runs were made, with and without mining as described in Mostyn et. al. (16). The GSI was estimated using the two modified Hoek-Brown criterion classification systems, RMR₈₉, Q and the Hoek-Brown chart given in Figure 6.

The results of the analysis using UDEC correlated well with the assumed failure mode. In Figure 7 the stresses predicted at failure by UDEC have been compared to those from the Hoek-Brown criteria. It is seen that the Hoek-Brown chart gives a higher estimate of the rock mass strength. The failure stresses appear to correspond reasonably to the lower bound estimated Hoek-Brown envelope.

The shear plane for the mining case showed failure both through the area of fictitious joints in the toe of the slope and through the coal seam. As the coal seam would have a different GSI to that estimated the stresses along both zones have been plotted separately. A Hoek-Brown envelope corresponding to a GSI of 25 for a crushed rock mass with fair to poor joint conditions has been plotted (the lowest curve on Figure 7). This envelope appears to correspond reasonably to the failure stresses obtained along the coal seam.

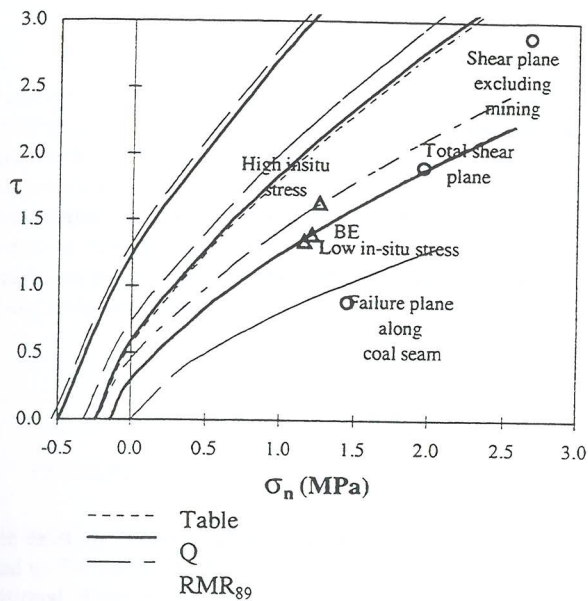


Figure 7: Hoek-Brown vs Estimated Stresses for Nattai

4.0 CONCLUSION

The case studies presented within this paper provide a first step towards a better understanding of the Hoek-Brown failure criterion. Further case studies are currently being analysed and results and conclusions will be presented as they become available. The authors are also involved in investigating the large scale in-situ shear strength of discontinuities. Due to the difficulty of obtaining good case studies on large scale discontinuity failures, only one defect case study has been attempted.

As has been shown in the case of Kidston Mine it is difficult to locate slopes that have failed through rock mass. This is particularly true for rock masses with a reasonably high GSI and/or intact rock strength.

The author would be grateful for any qualitative performance and rock mass characterisation data on rock masses that have failed or are near failure (both mass or defect controlled). If any reader is aware of such information do not hesitate to contact the author.

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3.6 References

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